
Efficient Probit Regression

Release 0.1.0

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Feb 06, 2022

API DOCUMENTATION

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This is the documentation of our code base.

EFFICIENT PROBIT REGRESSION API

Here you can find the documentation of most of our functions and classes.

1.1 Probit Model

```
class efficient_probit_regression.probit_model.PGeneralizedProbitSGD(p,
                                                                    initial_learning_rate=0.1,
                                                                    power_t=0.5)
```

Stochastic Gradient descent for probit regression. Adapts the learning rate in each iteration using inverse scaling.

Parameters

- **p** (*int*) – The order of the probit model.
- **initial_learning_rate** (*float*) – The initial learning rate.
- **power_t** (*float*) – Inverse scaling is used to adapt the learning rate in each iteration. The update formula is $\text{learning_rate} = \text{initial_learning_rate} / \text{power}(\text{cur_iteration}, \text{power_t})$

get_params()

The function get_params() returns the estimated parameters. (revision)

new_sample(x, y)

Performs one step of SGD on a new sample x, y.

Parameters

- **x** (*numpy.ndarray*) –
- **y** (*int*) –

```
class efficient_probit_regression.probit_model.ProbitSGD(initial_learning_rate=0.1, power_t=0.5)
```

Parameters

- **initial_learning_rate** (*float*) –
- **power_t** (*float*) –

```
efficient_probit_regression.probit_model.p_gen_norm_cdf(x, p)
```

Returns the cumulative density until a point x for $p \geq 1$.

```
efficient_probit_regression.probit_model.p_gen_norm_pdf(x, p)
```

Returns the density at a point x for $p \geq 1$.

1.2 Sampling

class `efficient_probit_regression.sampling.ReservoirSampler`(*sample_size*, *d*)

Implementation of a reservoir sampler as described in “A general purpose unequal probability sampling plan” by M. T. Chao, adapted here for row sampling of datasets consisting of a data matrix *X* and a label vector *y*.

Parameters

- **sample_size** (*int*) – Number of rows in the resulting sample.
- **d** (*int*) – Second dimension of the sample. The whole sample will have a dimension of (*sample_size*, *d*).

get_sample()

Returns the sample of *X* and the sample of *y*.

insert_record(*row*, *label*, *weight*)

Insert a data record consisting of a row and a label. The record will be sampled with a probability that is proportional to the given weight.

Parameters

- **row** (*numpy.ndarray*) –
- **label** (*float*) –
- **weight** (*float*) –

`efficient_probit_regression.sampling.compute_leverage_scores`(*X*, *p*=2, *fast_approx*=False)

Computes leverage scores.

Parameters *X* (*numpy.ndarray*) –

`efficient_probit_regression.sampling.fast_QR`(*X*, *p*=2)

Returns *Q* of a fast QR decomposition of *X*.

`efficient_probit_regression.sampling.leverage_score_sampling`(*X*, *y*, *sample_size*, *augmented*=False, *online*=False, *round_up*=False, *precomputed_scores*=None, *p*=2, *fast_approx*=False)

Draw a leverage score weighted sample of *X* and *y* without replacement.

Parameters

- **X** (*numpy.ndarray*) – Data matrix.
- **y** (*numpy.ndarray*) – Label vector.
- **sample_size** (*int*) – Sample size.
- **augmented** (*bool*) – Whether to add the additive $1/W$ term, where *W* is the sum of all weights.
- **online** (*bool*) – Compute online leverage scores in one pass over the data.
- **round_up** (*bool*) – Round the leverage scores up to the nearest power of two.
- **precomputed_scores** (*Optional[numpy.ndarray]*) – To avoid recomputing the leverage scores every time, pass the precomputed scores here.
- **p** (*int*) – The order of the *p*-generalized probit model.
- **fast_approx** (*bool*) – Whether to use the fast leverage score approximation algorithm.

Returns

X_reduced The reduced data matrix.

y_reduced The reduced label vector.

w The corresponding sample weights.

`efficient_probit_regression.sampling.logit_sampling(X, y, sample_size)`

Logit sampling from 2018 Paper On Coresets for Logistic Regression.

Returns X_reduced, y_reduced, weights

Parameters

- **X** (*numpy.ndarray*) –
- **y** (*numpy.ndarray*) –
- **sample_size** (*int*) –

`efficient_probit_regression.sampling.online_ridge_leverage_score_sampling(X, y, sample_size, augmentation_constant=None, lambda_ridge=1e-06)`

Sample X and y proportional to the online ridge leverage scores.

Parameters

- **X** (*numpy.ndarray*) –
- **y** (*numpy.ndarray*) –
- **sample_size** (*int*) –
- **augmentation_constant** (*Optional[float]*) –
- **lambda_ridge** (*float*) –

`efficient_probit_regression.sampling.truncated_normal(a, b, mean, std, size, random_state=None)`

Use rejection sampling if the interval [a, b] covers at least a probability mass of 5%. Otherwise use the implementation given in `scipy.stats.truncnorm`.

The parameters a and b specify the actual interval where the probability mass is located, mean and std specify the original normal distribution.

Parameters

- **a** (*numpy.ndarray*) –
- **b** (*numpy.ndarray*) –
- **mean** (*numpy.ndarray*) –
- **std** (*numpy.ndarray*) –

`efficient_probit_regression.sampling.uniform_sampling(X, y, sample_size)`

Draw a uniform sample of X and y without replacement.

Parameters

- **X** (*numpy.ndarray*) – A matrix of size (n, d).
- **y** (*numpy.ndarray*) – A vector of size (n,).
- **sample_size** (*int*) – The size of the sample that should be drawn.

Returns The reduced sample (X_reduced, y_reduced).

1.3 Datasets

```
class efficient_probit_regression.datasets.BaseDataset(add_intercept=True, use_caching=True,
                                                    cache_dir=None)

    get_X()
        Returns the data matrix from the data object.

    get_beta_opt(p)
        Returns the optimized/estimated parameters beta.

        Parameters p (int) – the order of the p-generalized probit-model.

        Returns returns the estimated parameters

    get_d()
        Returns the dimension of the data. d can also be regarded as the number of features.

    get_n()
        Returns the number of rows of the data.

    get_y()
        Returns the target data y.

class efficient_probit_regression.datasets.Coverttype(use_caching=True)
    Dataset Homepage: https://archive.ics.uci.edu/ml/datasets/Coverttype

    get_name()
        Returns name of the data set.

class efficient_probit_regression.datasets.Example2D

    get_name()
        Returns name of data set.

    load_X_y()
        Loads data set and returns X and y.

class efficient_probit_regression.datasets.Iris(use_caching=True)

    get_name()
        ” Returns name of data set.

    load_X_y()
        Loads data and returns X and y.

class efficient_probit_regression.datasets.KDDCup(use_caching=True)
    Dataset Homepage: https://kdd.ics.uci.edu/databases/kddcup99/kddcup99.html

    get_name()
        Returns name of data set.

class efficient_probit_regression.datasets.Webspam(drop_sparse_columns=True, use_caching=True)
    Dataset Source: https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/binary.html#webspam

    get_name()
        Returns name of data set.

    load_X_y()
        Loads data and returns X and y.

efficient_probit_regression.datasets.add_intercept(X)
    Adds intercept.
```

1.4 Experiments

```
class efficient_probit_regression.experiments.BaseExperiment(p, num_runs, min_size, max_size,  
                                                         step_size, dataset, results_filename)
```

Parameters

- **p** (*int*) –
- **num_runs** (*int*) –
- **min_size** (*int*) –
- **max_size** (*int*) –
- **step_size** (*int*) –
- **dataset** (`efficient_probit_regression.datasets.BaseDataset`) –
- **results_filename** (*str*) –

get_config_grid()

Returns a list of configurations that are used to run the experiments.

abstract get_reduced_X_y_weights(*config*)

Abstract method that each experiment overrides to return the reduced matrix X , label vector y and weights that correspond to an experimental config.

optimize(X, y, w)

Optimize the Probit regression problem given by X , y and w .

Parameters

- **X** – Data matrix.
- **y** – Label vector.
- **w** – Weights.

run(*parallel=False, n_jobs=4*)

Run the experiment.

Parallel = False parallel is set to False by default.

N_jobs = 4 n_jobs is set to 4 by default.

```
class efficient_probit_regression.experiments.BaseExperimentBayes(dataset, num_runs, min_size,  
                                                                max_size, step_size,  
                                                                prior_mean, prior_cov,  
                                                                samples_per_chain,  
                                                                num_chains, burn_in)
```

Parameters

- **dataset** (`efficient_probit_regression.datasets.BaseDataset`) –
- **num_runs** (*int*) –
- **min_size** (*int*) –
- **max_size** (*int*) –
- **step_size** (*int*) –
- **prior_mean** (`numpy.ndarray`) –

- **prior_cov** (*numpy.ndarray*) –
- **samples_per_chain** (*int*) –
- **num_chains** (*int*) –
- **burn_in** (*int*) –

abstract get_method_name()

Returns the name of the method, like “uniform”, “leverage”, or “leverage_online”.

```
class efficient_probit_regression.experiments.LeverageScoreSamplingExperiment(p, num_runs,  
                                                                           min_size,  
                                                                           max_size,  
                                                                           step_size,  
                                                                           dataset, re-  
                                                                           sults_filename,  
                                                                           only_compute_once=True,  
                                                                           online=False,  
                                                                           round_up=True,  
                                                                           fast_approx=False)
```

Parameters dataset ([efficient_probit_regression.datasets.BaseDataset](#)) –

get_reduced_X_y_weights (*config*)

Returns reduced X, y and weights.

run (***kwargs*)

Run the experiment.

Parallel = False parallel is set to False by default.

N_jobs = 4 n_jobs is set to 4 by default.

```
class efficient_probit_regression.experiments.LeverageScoreSamplingExperimentBayes(dataset,  
                                                                           num_runs,  
                                                                           min_size,  
                                                                           max_size,  
                                                                           step_size,  
                                                                           prior_mean,  
                                                                           prior_cov,  
                                                                           sam-  
                                                                           ples_per_chain,  
                                                                           num_chains,  
                                                                           burn_in)
```

Parameters

- **dataset** ([efficient_probit_regression.datasets.BaseDataset](#)) –
- **num_runs** (*int*) –
- **min_size** (*int*) –
- **max_size** (*int*) –
- **step_size** (*int*) –
- **prior_mean** (*numpy.ndarray*) –
- **prior_cov** (*numpy.ndarray*) –

- `samples_per_chain(int)` –
- `num_chains(int)` –
- `burn_in(int)` –

`get_method_name()`

Returns the name of the method, like “uniform”, “leverage”, or “leverage_online”.

```
class efficient_probit_regression.experiments.LewisSamplingExperiment(p, num_runs, min_size,
                                                                    max_size, step_size,
                                                                    dataset, results_filename,
                                                                    fast_approx=True)
```

Parameters `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –

`get_reduced_X_y_weights(config)`

Returns reduced X, y and weights.

```
class efficient_probit_regression.experiments.LogitSamplingExperiment(p, num_runs, min_size,
                                                                    max_size, step_size,
                                                                    dataset,
                                                                    results_filename)
```

Returns reduced X, y and weights.

Parameters

- `p(int)` –
- `num_runs(int)` –
- `min_size(int)` –
- `max_size(int)` –
- `step_size(int)` –
- `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –
- `results_filename(str)` –

`get_reduced_X_y_weights(config)`

Abstract method that each experiment overrides to return the reduced matrix X, label vector y and weights that correspond to an experimental config.

```
class efficient_probit_regression.experiments.OfflineLeverageScoreSamplingExperimentBayes(dataset,
                                                                                          num_runs,
                                                                                          min_size,
                                                                                          max_size,
                                                                                          step_size,
                                                                                          prior_mean,
                                                                                          prior_cov,
                                                                                          sam-
                                                                                          ples_per_chain,
                                                                                          num_chains,
                                                                                          burn_in)
```

Parameters

- `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –
- `num_runs(int)` –

- `min_size(int)` –
- `max_size(int)` –
- `step_size(int)` –
- `prior_mean(numpy.ndarray)` –
- `prior_cov(numpy.ndarray)` –
- `samples_per_chain(int)` –
- `num_chains(int)` –
- `burn_in(int)` –

`get_method_name()`

Returns the name of the method, like “uniform”, “leverage”, or “leverage_online”.

```
class efficient_probit_regression.experiments.OnlineRidgeLeverageScoreSamplingExperiment(p,  
                                                                                          num_runs,  
                                                                                          min_size,  
                                                                                          max_size,  
                                                                                          step_size,  
                                                                                          dataset,  
                                                                                          re-  
                                                                                          sults_filename)
```

Parameters `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –

`get_reduced_X_y_weights(config)`

Returns reduced X, y and weights.

```
class efficient_probit_regression.experiments.SGDExperiment(p, num_runs, min_size, max_size,  
                                                           step_size, dataset, results_filename)
```

Parameters `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –

`get_reduced_X_y_weights(config)`

In SGD, no reduction is performed.

`optimize(X, y, w)`

Applies SGD in one pass over the data.

```
class efficient_probit_regression.experiments.UniformSamplingExperiment(p, num_runs,  
                                                                        min_size, max_size,  
                                                                        step_size, dataset,  
                                                                        results_filename)
```

Parameters `dataset` (`efficient_probit_regression.datasets.BaseDataset`) –

`get_reduced_X_y_weights(config)`

Reduces the sample weights and returns them.

```
class efficient_probit_regression.experiments.UniformSamplingExperimentBayes(dataset,  
                                                                           num_runs,  
                                                                           min_size,  
                                                                           max_size,  
                                                                           step_size,  
                                                                           prior_mean,  
                                                                           prior_cov, sam-  
                                                                           ples_per_chain,  
                                                                           num_chains,  
                                                                           burn_in)
```

Parameters

- **dataset** (`efficient_probit_regression.datasets.BaseDataset`) –
- **num_runs** (`int`) –
- **min_size** (`int`) –
- **max_size** (`int`) –
- **step_size** (`int`) –
- **prior_mean** (`numpy.ndarray`) –
- **prior_cov** (`numpy.ndarray`) –
- **samples_per_chain** (`int`) –
- **num_chains** (`int`) –
- **burn_in** (`int`) –

get_method_name()

Returns the name of the method, like “uniform”, “leverage”, or “leverage_online”.

1.5 Settings

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